

TRIAC Dimmable LED Driver Using PIC12HV752



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INTRODUCTION

This technical brief describes a LED driver solution that is compatible with a traditional TRIAC dimmer. Microchip's PIC12HV752 microcontroller manages the whole circuit solution with a minimal firmware code.

The PIC12HV752 is a low-cost 8-pin chip with on-chip core independent peripherals that are suitable for power conversion applications. These peripherals are the Complementary Output waveform Generator (COG) and the Hardware Limit Timer (HLT). Other peripherals include I/O ports, a Fixed Voltage Reference (FVR), Comparators, a Digital-to-Analog Converter (DAC), Timers, a Capture/Compare/PWM (CCP) and an Analog-to-Digital Converter (ADC).

The solution described in this technical brief has the following specifications:

- TRIAC Dimmable
- Active 0.95 Power Factor Correction (PFC)
- 90-240 VAC Input
- 20 VDC/325 mA max. output

HIGH PF FLYBACK CONVERTER

The design solution which will be discussed in this technical brief uses a high Power Factor (PF) flyback converter operating in Critical Conduction Mode (boundary between continuous and discontinuous Inductor Current mode). This topology is basically a conventional flyback, except that it does not have a bulk capacitor after the full-bridge rectifier. The absence of the bulk capacitor allows the rectified sinusoid to be used as input of the converter rather than a fixed DC voltage.

What makes this topology an attractive solution for a TRIAC Dimmable application is its inherent Power Factor Correction (PFC). The incandescent lamp works well with a TRIAC dimmer because it is purely resistive. Therefore, in order to design a LED driver compatible with TRIAC dimmer, the input characteristics of the LED driver should be resistive, too. PFC can make the LED driver look like a pure resistor from the AC input side by making the input line current in-phase with the input line voltage.

Aside from the high PF, there are other advantages this topology can offer. The advantages can be summarized as follows:

- Isolation between the AC mains and the converter output (this is desirable for safety requirements)
- Minimizes the needs of heat sinks. Critical Conduction Mode (CrCM) ensures low switching losses of the MOSFET
- High PF reduces dissipation in the bridge rectifier

- ## THEORY OF OPERATION

MOSFET (Q1). The rising edge of the PWM is controlled by the HLT or the C1 comparator, while the falling edge is controlled by the C2 comparator. The input of C1 is derived from the voltage of the auxiliary winding of transformer T1, which is compared with V_{SS} to detect the zero crossing of the auxiliary winding voltage (V_{AUX}). The input of C2 is voltage across the R_{SENSE} resistor, which is compared to the DAC output. The DAC output depends on its V_{REF} , which is connected to the input wave shape signal, derived from the rectified input signal through a simple voltage divider.

- The line voltage is perfectly sinusoidal
- All components are ideal
- Zero-current detection delay is negligible

When applying the AC input voltage, the base voltage of transistor Q4 in the bootstrap circuit shown in [Figure 2](#) is increasing. When there is enough base voltage, Q4 turns on and diode (D14) is forward biased. The voltage across the base of Q4 is held up to 10V by Zener diode D13. When Q4 turns on, the collector current flows through R_C and D14 to increase the V_{DD} of the PIC12HV752. When V_{DD} is high enough (usually the minimum V_{DD} of the microcontroller) HLT, COG, DAC, ADC and comparators are initialized. After initialization, the HLT emits a pulse at 58 kHz to turn on Q1 initially. This will energize the primary inductance of T1 and transfer the magnetizing current to produce

V_{AUX} when Q1 turns off. Once the rectified V_{AUX} has reached 10 Volts, the forward voltage of D14 drops below 0.7 Volts. This allows D14 not to conduct and Q4 to turn off. Once Q4 is off, V_{DD} is supplied by V_{AUX} . It is important that Q4 always be off during normal circuit operation to avoid power dissipation on Q4. Q4 remains off as long as there is enough V_{AUX} . The operation of the bootstrap circuit is depicted through the waveform shown in Figure 3.

FIGURE 2: BOOTSTRAP CIRCUIT

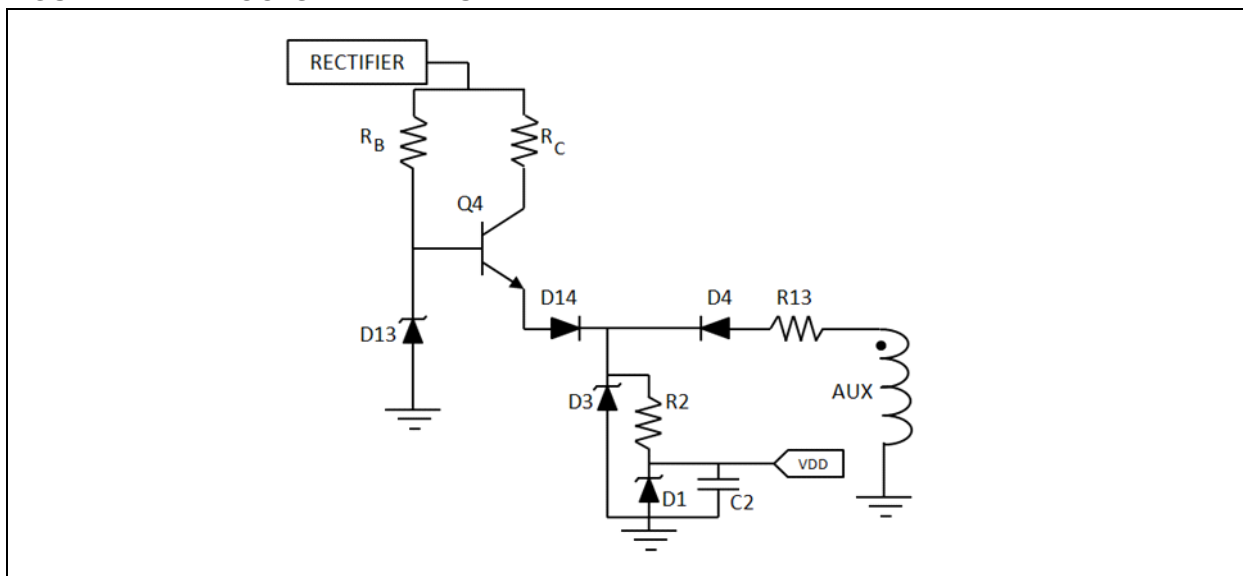
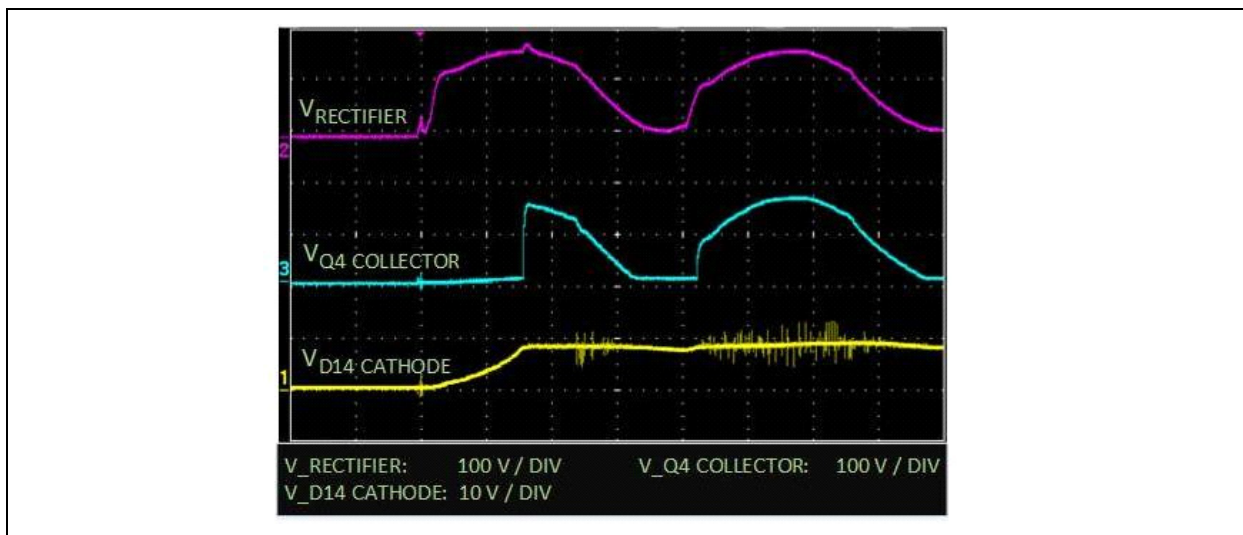


FIGURE 3: BOOTSTRAP WAVEFORM



Steady State Operation

When Q1 is on, the secondary diode (D2) is off and the voltage across the T1 primary magnetizing inductance (V_{LP}) is equal to $V_{IN}(t)$ (see Equation 1). $V_{IN}(t)$ is the rectified input voltage which is equal to peak input voltage (V_{PK}) multiplied by the rectified input line phase angle $2\pi f_L t$ ($f_L = 1/T_L$; f_L is the line voltage frequency and T_L is the line voltage period). To simplify the notation, let $2\pi f_L t$ be equal to θ (see Equation 2).

EQUATION 1: PRIMARY MAGNETIZING INDUCTANCE VOLTAGE

$$V_{LP} = V_{IN}(t)$$

EQUATION 2: INPUT VOLTAGE

$$V_{IN}(t) = V_{PK} * |\sin \theta|$$

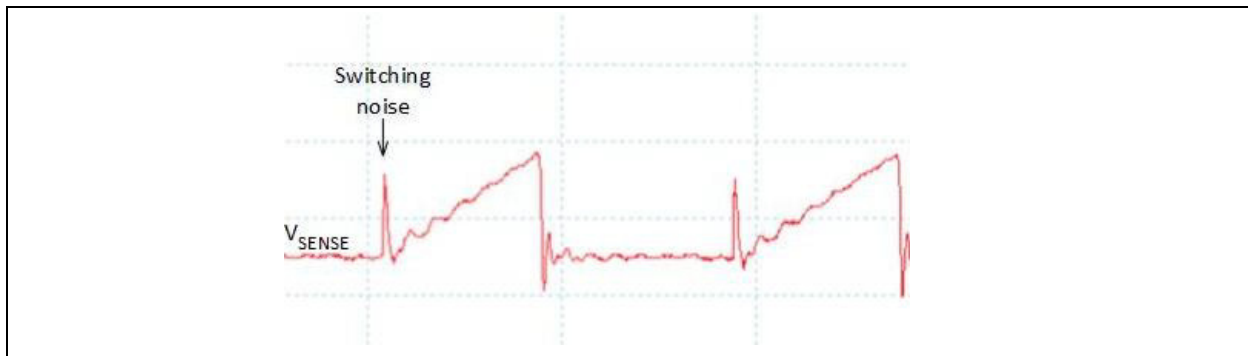
Additionally, when Q1 is on the primary inductance current (I_{LP}) is increasing linearly. This current will flow through the R_{SENSE} resistor. The voltage drop across R_{SENSE} is used as a sense voltage (V_{SENSE}) to translate I_{LP} (see Equation 3).

EQUATION 3: VOLTAGE ACROSS RSENSE

$$V_{SENSE} = R_{SENSE} * I_{LP}$$

Due to the turn-on event of Q1, I_{LP} is usually affected by a noise which is eventually reflected to V_{SENSE} (see Figure 4). In order to prevent this switching noise from causing a false trigger, the COG peripheral uses the comparator blanking timers to count off a few cycles.

FIGURE 4: SWITCHING NOISE ON VSENSE



V_{SENSE} is compared with the DAC voltage (V_{DAC}) (this is also the peak current set point) by the C2 comparator. V_{DAC} is derived from the rectified input voltage through a voltage divider so that it follows the rectified input and forces the peak current of primary inductance (I_{LPK}) to be synchronized and proportional to the rectified input. This is how the circuit achieves the PFC function. Equation 4 represents the V_{DAC} voltage.

EQUATION 4: DAC VOLTAGE

$$V_{DAC} = V_{PK} * |\sin \theta| \left(\frac{R_{REF}}{R1 + R_{REF}} \right) \left(\frac{DAC < 0: 4 >}{2^5} \right)$$

When V_{SENSE} reaches V_{DAC} , Q1 turns off and HLT is reset. The duration while Q1 is on (T_{ON}) can be derived using Equation 1. V_{LP} in Equation 1 is equal to the primary inductance (L_P) multiplied by the rate of change of I_{LP} with respect to time. Equation 5 shows this relationship.

EQUATION 5: PRIMARY MAGNETIZING INDUCTANCE VOLTAGE

$$V_{PK} * |\sin \theta| = L_P \frac{dI_{LP}}{dt}$$

Deriving the primary inductance current with respect to V_{PK} leads to Equation 6.

EQUATION 6: PRIMARY INDUCTANCE CURRENT

$$I_{LP} = \int_0^{T_{ON}} \frac{V_{PK} |\sin \theta|}{L_P} dt = \frac{V_{PK} |\sin \theta| T_{ON}}{L_P}$$

I_{LP} is also equal to $I_{PK} \sin \theta$ since the I_{PK} is enveloped by the rectified sinusoid. Using this relationship and Equation 6 we can solve T_{ON} (see Equation 7).

EQUATION 7: Q1 TURN-ON TIME

$$T_{ON} = \frac{L_P I_{PK} |\sin \theta|}{V_{PK} |\sin \theta|} = \frac{L_P I_{PK}}{V_{PK}}$$

It can be observed in Equation 7 that T_{ON} is not affected by the θ phase angle. Therefore, T_{ON} is constant over the instantaneous line cycle. However, T_{ON} tends not to become constant at minimum voltage on both sides of the rectified sinusoid. This is due to a slight input offset caused by Peak Current mode control comparator C2.

When Q1 is off, D2 is on and the voltage output (V_O) is equal to the voltage of T1 secondary inductance winding (V_{LS}). The primary magnetizing current is transferred to the secondary winding as secondary inductance current (I_{LS}). The I_{LS} decreases linearly and the duration time before it reaches zero is defined by T_{OFF} (see Equation 8 to Equation 10 in deriving T_{OFF}).

Using Equation 8, I_{LS} current can be derived as shown in Equation 9.

EQUATION 8: VOLTAGE OUTPUT

$$V_O = V_{LS} = L_S \frac{dI_{LS}}{dt}$$

EQUATION 9: SECONDARY MAGNETIZING CURRENT

$$I_{LS} = \int_0^{T_{OFF}} \frac{V_O}{L_S} dt = \frac{V_O T_{OFF}}{L_S}$$

I_{LS} is also equal to $n I_{PK} \sin \theta$ and L_S is equal to L_P/n^2 where n is T1's primary to secondary winding turns ratio N_P/N_S . Substituting to Equation 9 and solving for T_{OFF} yields to Equation 10 below.

EQUATION 10: Q1 TURN-OFF TIME

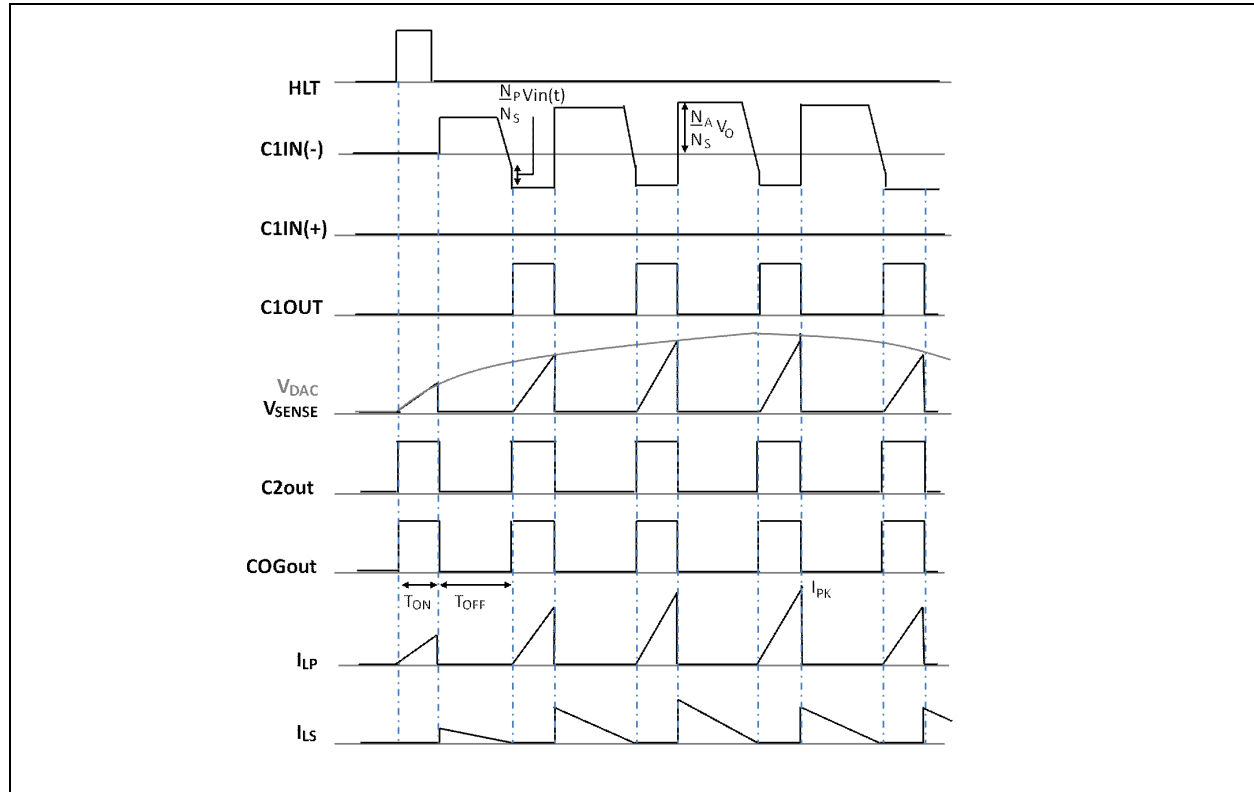
$$T_{OFF} = \frac{\frac{L_P}{n^2} n I_{PK} |\sin \theta|}{V_O} = \frac{L_P I_{PK} |\sin \theta|}{n V_O}$$

In Equation 10, T_{OFF} is a function of θ , therefore, it is variable over the instantaneous line cycle.

As stated earlier, the design is working in CrCM. In order to ensure this conduction mode operation, Q1 should turn on again when I_{LS} reaches zero. This is made possible through zero current detection (ZCD) using C1. C1 detects I_{LS} zero crossing based on V_{AUX} .

Figure 5 shows a timing diagram to visualize the control operation from start-up to steady state.

FIGURE 5: LED DRIVER CONTROL TIMING DIAGRAM



Since the circuit works at CrCM the sum of Equation 7 and Equation 10 is equal to the switching period T_S (see Equation 11).

EQUATION 11: Q1 SWITCHING PERIOD

$$T_S = T_{ON} + T_{OFF} = \frac{L_P I_{PK}}{V_{PK}} \left[1 + \frac{V_{PK} |\sin \theta|}{n V_O} \right]$$

The switching frequency F_S is the inverse of T_S shown in Equation 12.

EQUATION 12: Q1 SWITCHING FREQUENCY

$$F_S = \frac{V_{PK}}{L_P I_{PK}} \cdot \frac{1}{1 + \frac{V_{PK} |\sin \theta|}{n V_O}}$$

In Equation 12, it is observable that F_S varies with the instantaneous line voltage since it is a function of θ . The switching Duty Cycle (D) is the ratio between T_{ON} and T_S , and varies with instantaneous voltage as well (see Equation 13).

EQUATION 13: DUTY CYCLE

$$D = \frac{T_{ON}}{T_S} = \frac{1}{1 + \frac{V_{PK} |\sin \theta|}{n V_O}}$$

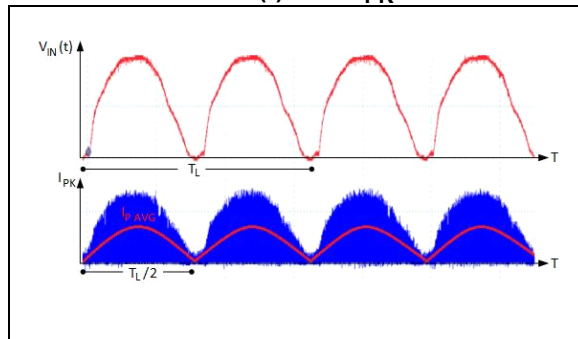
Power Transfer

The average input current ($I_{P\text{ AVG}}$) can be obtained by averaging the area under I_{LP} (see Equation 14). This current is sinusoidal and in-phase with $V_{IN}(t)$. As a result, the LED driver behaves much like a resistor and exhibits a PF close to unity (see Figure 6).

EQUATION 14: AVERAGE INPUT CURRENT

$$I_{P\text{ AVG}} = \frac{1}{2} I_{PK} |\sin \theta| D = \frac{1}{2} \frac{V_{PK} |\sin \theta| D^2 T_S}{L_P}$$

FIGURE 6: $V_{IN}(t)$ AND I_{PK} WAVEFORM



The input power, $P_{IN\text{ AVG}}$, drawn by the LED driver is derived by averaging the product of $V_{IN}(t)$ and $I_{P\text{ AVG}}$ over one half line cycle T_L (see Equation 15).

EQUATION 15: AVERAGE INPUT POWER

$$P_{IN\text{ AVG}} = \int_0^{T_L/2} V_{IN}(t) I_{P\text{ AVG}} dt = \frac{1}{4} \frac{V_{PK}^2 D^2 T_S}{L_P}$$

$P_{IN\text{ AVG}}$ can be a function of $V_{IN\text{ RMS}}$ (see Equation 16).

EQUATION 16: AVERAGE INPUT POWER WITH RESPECT TO INPUT RMS VOLTAGE

$$P_{IN\text{ AVG}} = \frac{V_{IN\text{ RMS}}^2}{\left(\frac{2 L_P}{D^2 T_S}\right)} = \frac{V_{IN\text{ RMS}}^2}{R_{EFFECTIVE}} ; R_{EFFECTIVE} = \frac{2 L_P}{D^2 T_S}$$

In Equation 16, $R_{EFFECTIVE}$ is the input equivalent resistance of the LED driver seen by the AC main input.

In order to relate the $P_{IN\text{ AVG}}$ to LED average current I_{LED} , the relationship of output power P_O with input power P_{IN} of LED driver will be used. This relationship is defined on Equation 17.

EQUATION 17: OUTPUT POWER

$$P_O = \eta P_{IN}$$

In Equation 17, P_O is equal to the product of V_O and I_{LED} where V_O is also equal to the LED string forward voltage. P_{IN} is equal to $P_{IN\text{ AVG}}$ and η is the efficiency of the LED driver. Deriving the equation for I_{LED} from this relationship leads to Equation 18.

EQUATION 18: LED CURRENT

$$I_{LED} = \eta \frac{V_{IN\text{ RMS}}^2}{V_O R_{EFFECTIVE}}$$

In Equation 18, I_{LED} is function of $V_{IN\text{ RMS}}$. This is the same RMS voltage that the TRIAC dimmer alters when dimming the LED. Therefore, through the relationship between I_{LED} and V_{RMS} shown in Equation 18, LED brightness can be controlled by the TRIAC dimmer.

ADDITIONAL CIRCUIT

In [Figure 1](#), there are some circuit blocks included in the design in order to improve the reliability.

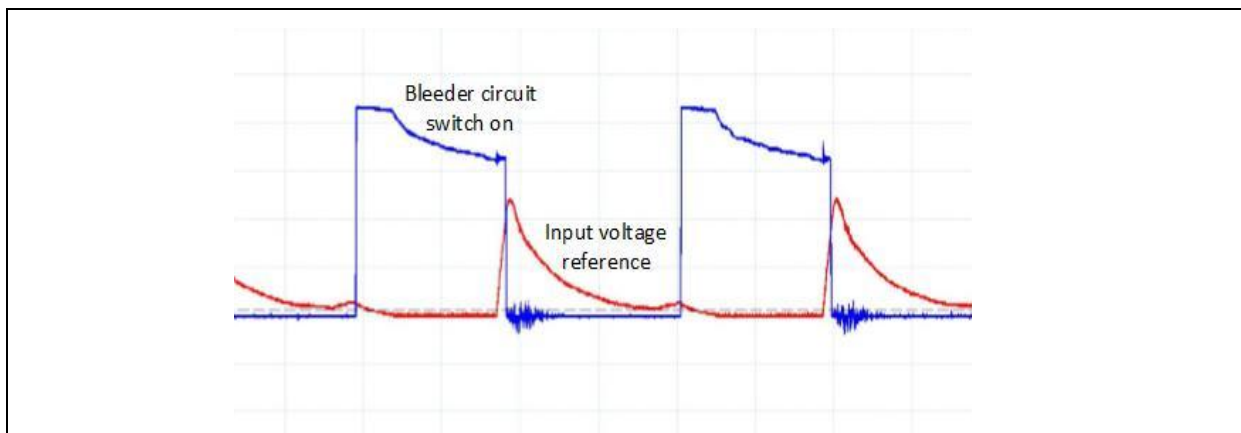
Inrush Current Circuit

The Inrush current circuit is an active circuit that protects the primary side components by suppressing the large input current spikes. These large current spikes are induced in the input line when the TRIAC in the dimmer is fired. A large spike will also create an input current oscillation that may cause the TRIAC to misfire.

Bleeder Circuit

The bleeder circuit draws additional current in order to maintain the TRIAC holding current at low input line voltage. Not maintaining the required holding current of the TRIAC will cause the TRIAC to misfire. The circuit is composed of the bleeder resistor and a bipolar transistor, which is turned on by the microcontroller only when certain rectified low input voltage is detected through the ADC. This is an efficient way to implement a bleeder since it will not consume additional power when it is not needed. [Figure 7](#) shows the switching timing of the bleeder circuit.

FIGURE 7: SWITCHING OF BLEEDER CIRCUIT



Snubber Circuit

The snubber circuit is used to protect Q1 from a large voltage spike caused by the leakage inductance of T1. When Q1 turns off, the energy from the leakage inductance is reflected back to primary winding. The snubber circuit dissipates this energy to minimize the voltage spike. The circuit consists of a fast switching diode in series with a parallel combination of a capacitor and resistor. In some designs, an additional Zener transil clamp is included to minimize the power loss at light load.

ACTUAL CIRCUIT

The actual circuit of the TRIAC Dimmable LED Driver is provided in [Appendix B: “LED Driver Schematic”](#). The value of components shown are to be treated only as a starting point. They need to be tuned for each design. The design must be verified and optimized across the entire range of operating conditions.

FIRMWARE

The circuit design of the LED driver seems complex as it appears but the firmware is straightforward (see [Figure 8](#)). It appears that the firmware's overhead is small and mainly consists of initializing the core independent peripherals. The pins on the PIC[®] device are configured according to their function. After the pins have been configured, the peripherals are setup and turned on. During the initialization, the internal connections and functions of the peripherals are established. The ADC detects the status of the TRIAC dimmer. If the rectified input voltage sampled by the ADC exceeds the TRIAC minimum holding current threshold voltage, the bleeder circuit turns off, otherwise, it will turn on. Before the bleeder circuit turns on, a certain delay is required to evaluate the state of TRIAC dimmer.

```

graph TD
    START([START]) --> Config[Configure pin function]
    Config --> InitComp[Initialize the two Comparators]
    InitComp --> InitHLT[Initialize HLT]
    InitHLT --> InitCOG[Initialize COG]
    InitCOG --> InitDAC[Initialize DAC]
    InitDAC --> InitADC[Initialize ADC]
    InitADC --> A1((A))
    A1 --> Decision{Is the rectified input voltage sampled by ADC > triac threshold?}
    Decision -- YES --> TurnOff[Turn off bleeder circuit (RAO = 0)]
    TurnOff --> A2((A))
    Decision -- No --> Delay[Bleeder_timer delay]
    Delay --> TurnOn[Turn on bleeder circuit (RAO = 1)]
    TurnOn --> A3((A))

```

Figure 9 and Table 1 summarize the MCU peripheral configuration.

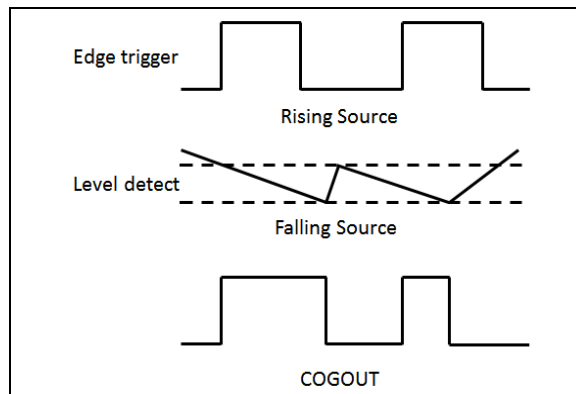
Pin No.	Name	Function	Circuit Connection
1	VDD	Supply Voltage	Bootstrap
2	C2IN-	Comparator 2 negative input	Sensing resistor
3	C1IN-	Comparator 1 negative input	Auxiliary regulated voltage
4	MCLR	Memory Clear	ICSP™ (In-Circuit Serial Programmer™)
5	COGOUT0	Complementary Output Generator	MOSFET Driver
6	AN1/VREF	Analog-to-Digital	Rectifier input voltage through voltage divider
7	I/O	Output	Bleeder circuit
8	VSS	Ground connection	Ground

COG (Complementary Output Generator)

The main purpose of the Complementary Output Generator (COG) in the circuit design is to convert two separate input events into a single PWM output. The COG uses two independently selectable event sources to generate the PWM. These event sources are the rising event, RS, and the falling event, FS, set by the two comparators and the HLT. The event input detection may be selected as level detection or edge-triggered. The rising source and falling source operate as edge-triggered and level sensitive, respectively.

COG output Q is set to high only when a rising edge triggers the rising source input. During this time, the COG turns on the MOSFET. The MOSFET turns off when a low-voltage level is detected on the falling source of the COG. Figure 10 describes the operation of the COG.

FIGURE 10: COG OPERATION



During MOSFET switching, noise may occur that could result in false triggering. This can be avoided by using a blanking scheme. Blanking disregards the event inputs for a short period of time. Since the oscillator of the PIC12HV752 runs at 8 MHz and the blanking count register is set to 4, the resulting blanking time would range from 500 ns to 625 ns on both falling and rising sources. Equation 19 describes the blanking calculation.

EQUATION 19: COG BLANKING RANGE

$$T_{min} = \frac{Count}{F_{COG_Clock}}; T_{max} = \frac{Count+1}{F_{COG_Clock}}$$

Where:

$$Count = \begin{cases} GxBLKR < 3:0 > = 4, & \text{rising event} \\ GxBLKF < 3:0 > = 4, & \text{falling event} \end{cases}$$

$$F_{COG_clock} = 8 \text{ MHz}$$

HLT (Hardware Limit Timer)

The primary purpose of the HLT is to act as a timed hardware limit to be used in conjunction with asynchronous analog feedback applications. The external Reset source synchronizes the HLT timer with the analog application.

When the external Reset source occurs before the HLT timer and HLT period match, the HLT timer resets for the next period and prevents its output from going active. However, if the external Reset source fails to generate a signal within the expected time, allowing the HLT timer and HLT period to match, then the HLT output becomes active.

The HLT is configured to be internally connected to the rising source of the COG. HLT provides a rising edge to the COG to initiate the start-up of the converter. The HLT time is set through the equation as shown below in Equation 20:

EQUATION 20: HLT TIME

$$HLT \text{ Time} = (HLTPR1 + 2) \left(\frac{4}{F_{osc}} \right)$$

Where: $HLTPR1 = 32$

$$F_{osc} = 8 \text{ MHz}$$

COMPARATORS

Comparators are used to interface analog circuits to a digital circuit by comparing two analog voltages and providing a digital indication of their relative magnitudes. The comparator outputs can be applied to the COG module and can be configured as a closed-loop analog feedback to the COG, thereby creating a PWM controlled in an analog way.

The output of C1 is ORed to the HLT and acts as the rising source of the COG, while the output of C2 is the falling source of the COG. These two comparators act as zero-cross detection and peak current detection on the circuit, respectively. The output of C1 continually resets HLT during the operation of the converter.

DAC (Digital-to-Analog Converter)

A 5-bit DAC module is used to translate the rectified input voltage. It is internally connected to the positive input of C2. It operates in Full-Range mode with the DAC output voltage as shown in Equation 21 where V_{SRC} is the voltage across the voltage divider network (see Figure 1).

EQUATION 21: DAC VOLTAGE

$$V_{DAC} = \left((V_{SRC} +) \left(\frac{DACR < 4:0 >}{2^5} \right) \right)$$

Where: $DACR < 4:0 > = \begin{cases} 1, & \text{at } 230V \\ 7, & \text{at } 115V \end{cases}$

ADC (Analog-to-Digital Converter)

The ADC converts the input signal into a 10-bit binary representation. This value is calculated using the ADC equation shown in [Equation 22](#).

The ADC samples and translates the rectified input voltage in order to control the toggling of pin 7 (RA0). RA0 becomes low when the voltage sampled by the ADC is greater than the minimum voltage required to maintain the holding current of the TRIAC dimmer, otherwise, RA0 will be high.

EQUATION 22: ADC VOLTAGE

$$V_{ADC} = \frac{V_{SRC}(2^{10} - 1)}{V_{ADC REF}}$$

PERFORMANCE

[Table 2](#) and [Table 3](#) show the measured dimming performance of the LED driver operating at 230V and 115V, respectively. Its graphical representation is shown in [Figure 11](#) wherein the dimming is controlled by the TRIAC output voltage.

TABLE 2: MEASURED DIMMING PERFORMANCE AT 230V INPUT VOLTAGE

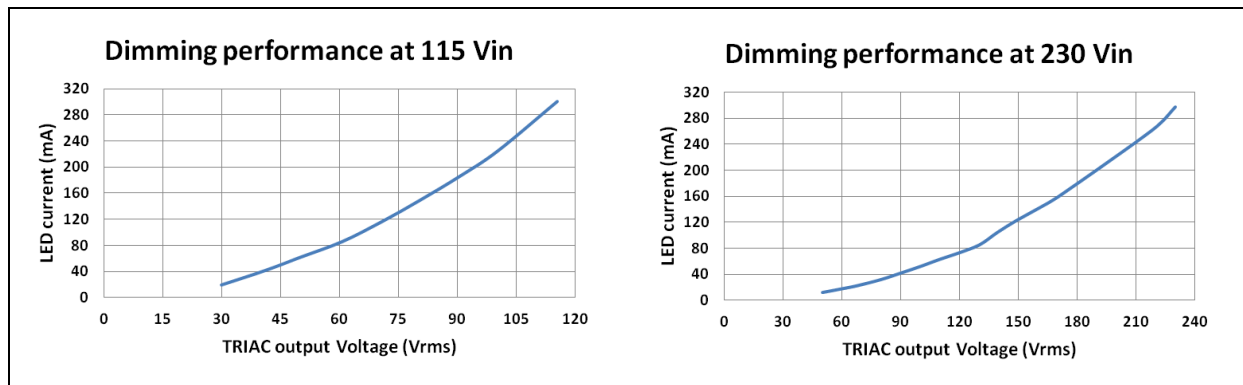
230 V _{IN}	
TRIAC Output Voltage (V _{RMS})	LED Current (mA)
230.1	297.33
218.5	262.21
172	162.63
160.1	141.03
149.1	122.81
139.4	104.57
130.1	85.16
119	72.24
109.8	62.9
101	53.11
90.1	41.95

TABLE 2: MEASURED DIMMING PERFORMANCE AT 230V INPUT VOLTAGE

230 V _{IN}	
TRIAC Output Voltage (V _{RMS})	LED Current (mA)
80.3	32.24
68.2	22.81
60.2	17.86
50.15	12.11

TABLE 3: MEASURED DIMMING PERFORMANCE AT 115V INPUT VOLTAGE

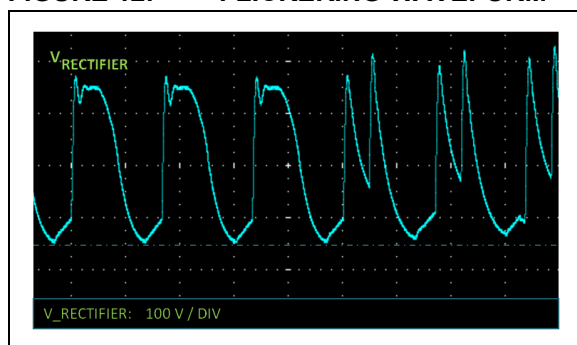
115 V _{IN}	
TRIAC Output Voltage (V _{RMS})	LED Current (mA)
115.5	300.39
100.5	225.22
90.8	186.03
80.5	148.73
70.7	115.49
60.7	85.23
50.23	61.65
41.2	41.19
29.99	18.84

FIGURE 11: DIMMING PERFORMANCE**POSSIBLE DESIGN IMPROVEMENTS**

Even a high Power Factor device like the LED driver discussed in this technical brief represents a capacitive load. This is because of the filter implemented at the input side of the circuit. This LC filter can produce a high voltage ringing derived from input current oscillation when the TRIAC in the dimmer initially fires. The voltage ringing makes the TRIAC current drop below the holding current and switch off and on again several times during the cycles, resulting in severe flickering and a humming sound.

CONCLUSION

This technical brief describes a PIC microcontroller-based solution controlling the LED driver that is compatible with traditional TRIAC dimmers. With the PIC12HV752, the analog control mainly runs by itself and only requires small firmware overhead. This enables users to add algorithms in order to improve design performance, bring intelligence to the system, or measure any parameter.

FIGURE 12: FLICKERING WAVEFORM

During the first three cycles in the rectified line voltage shown in Figure 12, the TRIAC has recovered after firing and continues the conduction. However, after the three cycles, the rectified input waveform changed showing that the TRIAC is turning on and off. This input line event produces flickering and a humming sound.

For a smooth dimming and a quiet operation, the challenge is to avoid unwanted TRIAC switching, caused by the ringing that occurs when the TRIAC is initially fired. The input filter of the LED driver design presented in this technical brief requires an optimization to avoid this problem and ensures that the line waveform will not be altered.

APPENDIX A: LED DRIVER EQUATION DERIVATION

EXAMPLE A-1: $I_{P\text{ AVG}}$ DERIVATION

$$V = \frac{L di}{dt}$$

$$di = \frac{v dt}{L}$$

$$I_{PK} = \frac{V_{IN}(t)}{L_P} D T_S$$

Where: $V_{IN}(t) = V_{PK} \sin(2\pi f_L t)$

Let $f_L = \frac{1}{T_L}$

$$V_{IN}(t) = V_{PK} \sin\left(\frac{2\pi t}{T_L}\right)$$

Substitute $V_{IN}(t)$ to I_{PK} equation

$$I_{PK} = \frac{V_{PK} \sin\left(\frac{2\pi t}{T_L}\right)}{L_P} D T_S$$

To get the average input current, the equation below must be evaluated

$$I_{P\text{ AVG}} = \frac{1}{T_S} \int_0^{T_S} \frac{1}{2} I_{PK} dt$$

$$I_{P\text{ AVG}} = \frac{1}{T_S} \times \frac{1}{2} \times I_{PK} \int_0^{T_S} dt$$

Integrating and Substituting I_{PK} to the equation

$$I_{P\text{ AVG}} = \frac{1}{T_S} \times \frac{1}{2} \times \frac{V_{IN}(t)}{L_P} D T_S \left[\int_0^{D T_S} dt - \int_{D T_S}^{T_S} 0 dt \right]$$

$$I_{P\text{ AVG}} = \frac{1}{T_S} \times \frac{1}{2} \times \frac{V_{IN}(t)}{L_P} D T_S \times D T_S$$

Simplifying the equation results to:

$$I_{P\text{ AVG}} = \frac{V_{IN}(t)}{2 L_P} D^2 T_S$$

EXAMPLE A-2: $P_{IN\ AVG}$ DERIVATION (CONTINUED)

$$P_{IN\ AVG} = \frac{2}{T_L} \int_0^{\frac{T_L}{2}} V_{IN}(t) I_{IN}(t) dt$$

$$P_{IN\ AVG} = \frac{2}{T_L} \int_0^{\frac{T_L}{2}} \frac{V_{PK}^2 \sin^2\left(\frac{2\pi t}{T_L}\right) D^2 T_S}{2L_P} dt$$

$$P_{IN\ AVG} = \frac{2}{T_L} \frac{V_{PK}^2 D^2 T_S}{2L_P} \int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt$$

Solve for the integral equation: $\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt$

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \int_0^{\frac{T_L}{2}} \frac{1 - \cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt$$

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \int_0^{\frac{T_L}{2}} \frac{1}{2} dt - \int_0^{\frac{T_L}{2}} \frac{\cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt$$

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \frac{1}{2} t \Big|_0^{\frac{T_L}{2}} - \frac{1}{2} \int_0^{\frac{T_L}{2}} \cos 2\left(\frac{2\pi t}{T_L}\right) dt$$

Simplify the integral equation $\int_0^{\frac{T_L}{2}} \frac{\cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt$ by letting:

$$u = 2\left(\frac{2\pi t}{T_L}\right) = \frac{4\pi t}{T_L}$$

Derivative of u results to:

$$du = \frac{4\pi}{T_L} dt$$

Simplified equation for $\int_0^{\frac{T_L}{2}} \frac{\cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt$ is:

$$\int_0^{\frac{T_L}{2}} \frac{\cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt = \frac{1}{2} \int_0^{\frac{T_L}{2}} \cos u du$$

$$\frac{1}{2} \int_0^{\frac{T_L}{2}} \cos u du = \frac{1}{2} \sin u + c$$

$$\frac{1}{2} \int_0^{\frac{T_L}{2}} \frac{\cos 2\left(\frac{2\pi t}{T_L}\right)}{2} dt = \frac{1}{2} \sin \frac{4\pi t}{T_L} \Big|_0^{\frac{T_L}{2}}$$

Substitute to the resulted value to $\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt$:

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \frac{1}{2} t \Big|_0^{\frac{T_L}{2}} - \frac{1}{2} \sin \frac{4\pi t}{T_L} \Big|_0^{\frac{T_L}{2}}$$

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \frac{1}{2} \left(\frac{T_L}{2} - 0\right) - \frac{1}{2} \left(\sin \frac{4\pi \left(\frac{T_L}{2}\right)}{T_L} - \sin 0\right)$$

EXAMPLE A-3: $P_{IN\ AVG}$ DERIVATION (CONTINUED)

$$\int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt = \frac{T_L}{4}$$

Substitute to $P_{IN\ AVG}$ equation:

$$P_{IN\ AVG} = \frac{2}{T_L} \frac{V_{PK}^2 D^2 T_S}{2L_P} \int_0^{\frac{T_L}{2}} \sin^2\left(\frac{2\pi t}{T_L}\right) dt$$

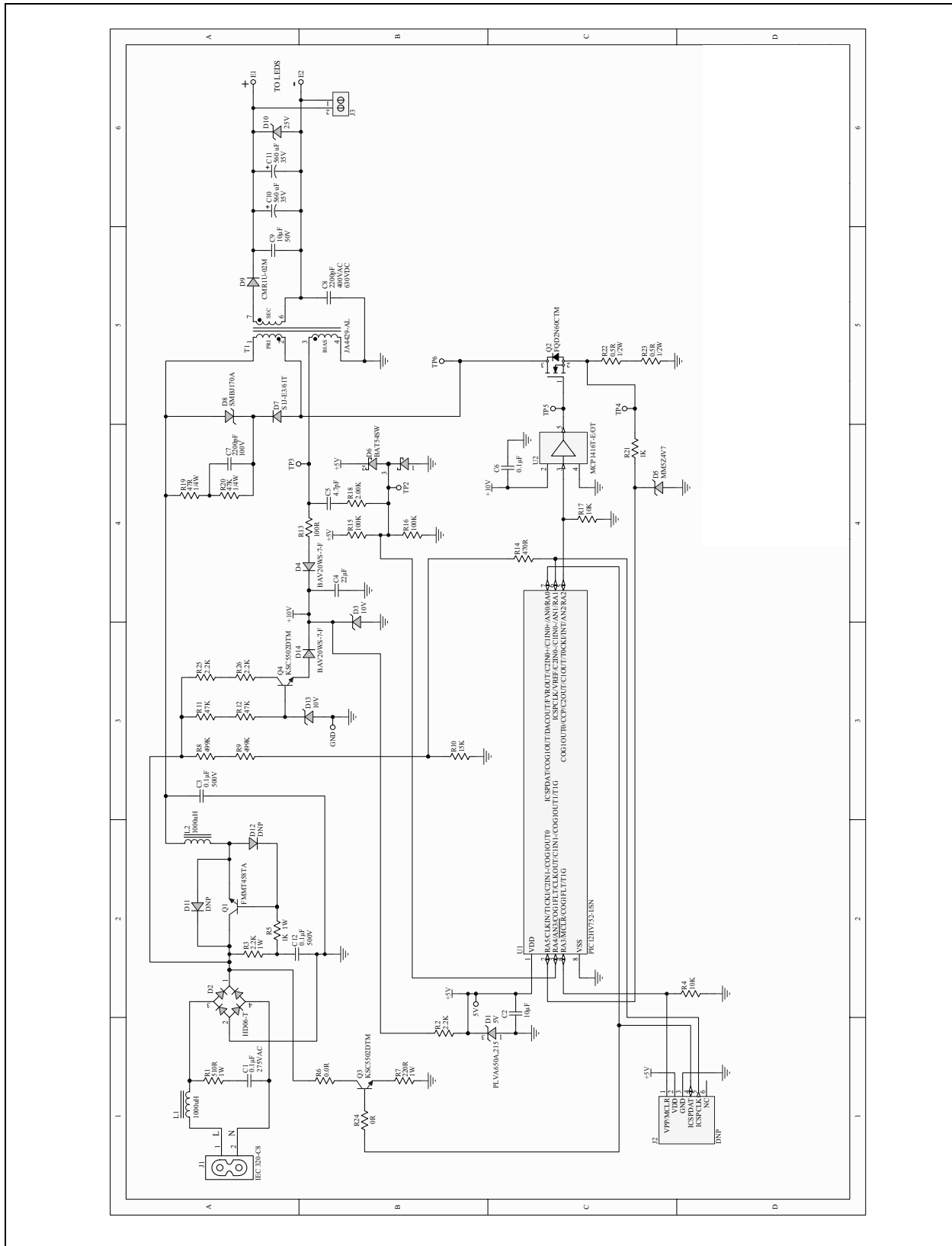
$$P_{IN\ AVG} = \frac{2}{T_L} \frac{V_{PK}^2 D^2 T_S}{2L_P} \left(\frac{T_L}{4}\right)$$

$P_{IN\ AVG}$ results to:

$$P_{IN\ AVG} = \frac{V_{PK}^2 D^2 T_S}{4L_P}$$

APPENDIX B: LED DRIVER SCHEMATIC

FIGURE B-1: TRIAC DIMMABLE LED DRIVER SCHEMATIC



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